

m3f22cw(1718)

**F22 ASSESSED COURSEWORK. 17.11.2017**

Deadline 1.12.2017, 4pm.

In a three-period binomial model, the stock price goes up by a factor of  $u = 6/5$  with probability  $p \in (0, 1)$ , or down by a factor of  $d = 5/6$  with probability  $1 - p$ . The initial stock price is 60. Neglect interest.

- (i) Find the martingale probability  $p^*$ .
- (ii) Price a European call option with expiry time  $T = 3$  with strike  $K = 50$ .
- (iii) Price the corresponding American option, and find the early-exercise and continuation regions.
- (iv) Repeat (ii) and (iii) with  $K = 70$ .
- (v) Comment on the difference between the  $K = 50$  and 70 results.

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